

Evacuation System in a Building Using Cellular Automata for Pedestrian Dynamics

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Abstract

The sense of safety in public facilities for pedestrians can be shown by the availability of good infrastructure, particularly the building. One of the aspects that can make pedestrians feel comfortable and safe is the availability of evacuation facilities in emergency situation. When a disaster strikes, people would start to panic and this will cause problems, especially during an evacuation. During panic in an evacuation process, pedestrians tend to act blindly and walk randomly and mindlessly. They might follow one another when they get panic. This is called as *herding behavior*. Regarding the evacuation systems, cellular automata is the basic method used to represent human motion. The movement of pedestrian is an important aspect during an evacuation process and this can be analyzed and implemented by using *Cellular Automata*. It is a simple method yet it can solve complex problems. Total evacuation time becomes the indicators in measuring the efficiency of this system. The result of comparison method shows that the proposed method could work better in certain conditions. In addition, the results of the experiments during panic and normal situation show similar characteristics especially regarding density aspect, yet evacuation time during panic situation takes longer time. The experiment's results by using the actual data also has similar tendency with the evacuation time.

Keywords: evacuation time, cellular automata, panic behavior, pedestrian

1. INTRODUCTION

Indonesia is one of the countries with relatively high frequency of disasters. Every year, the number of the victims of the disaster is quite high. Most of the casualties are caused by the fall of buildings. Many high-rise buildings in Indonesia do not have good evacuation standards. This condition would potentially cause the higher number of victims when a disaster occurs. When such disaster occurs, the problem not only lies in whether or not there

are good evacuation facilities and procedures, but also the individuals themselves.

Pedestrian flow modeling based on cellular automata has been investigated by many researchers in understanding this phenomenon. Cellular automata is a discrete model suitable for modeling steps or movements of pedestrian. Pedestrian flow modeling consists of three methods: *continuum model*, *social force model*, and *cellular automata (CA) model*. The modeling and analysis of the macroscopic of pedestrian flow uses a continuum model. Three of the macroscopic variables of pedestrian includes *speed*, *density*, and *flow*. Some published papers of the macroscopic variables of pedestrian flow discuss about the continuum model [1][2][3][12]. A concept of continuum model for the flow of pedestrians including the equilibrium system was presented by [1] comparing the stability of disturbances in subcritical flows and supercritical flows, [2] revisiting Hughes's dynamics continuum model for pedestrian flow when it is performed, and [12] developing an efficient algorithm solution. The algorithm used time-varying for the pedestrian generation while the interaction of each variable includes *pedestrian density* and *flux*. Walking speed is performed by using conservation equation. An algorithm for an extended reactive dynamic user equilibrium model of pedestrian counterflow as a continuum is developed by [12]. It is based on a cell-centered high-resolution finite volume scheme with a fast sweeping method for an Eikonal-type equation on an orthogonal grid. The numerical results demonstrate the rationality of the model and efficiency of the algorithm.

C. Burstedde [1] has developed a model on evacuation process in large room to investigate the interaction between pedestrians. In line with that research, this study will simulate pedestrian movement in a building by using similar method with some modifications. This method uses cellular automata as the basic method for modeling and $v_{max}=1$ cell (*v max is velocity maximum of pedestrians*). According to the research presented by Dirk Heldbing [4], panic pedestrians will run faster than normal pedestrians. Therefore, this study will extend $v_{max}=2$ cells to represent the character of panic pedestrians.

2. RELATED WORKS

Several methods have been proposed to model pedestrians' behavior. Modeling pedestrians' behaviors during long-range interactions between pedestrian based on Cellular Automata are mediated by floor fields (*Cell of Cellular Automata Model*) and using chemotaxis approach (C. Burstedde 2001) [1]. The model only simulates pedestrian in a room. Modeling the characteristics of pedestrians during evacuation process is very complicated. Angsar Kirchner has developed new model in extending the model developed by C. Burstedde [1][2]. The model adds some parameter to C. Burstedde's model in analyzing herding and panic behavior of pedestrians.

During evacuation process, unexpected things might occur and pedestrians' behavior is unpredictable. In this condition many pedestrians will bump into each other. This study tries to investigate and solve the problem when two or more pedestrians try to enter the same space by using probability as a solution [1][3]. One of the important things during evacuation process is the behavior of pedestrian as affected by panics. Many people will feel scared and urged to find safe places while determining what to do. Dirk Helbing [4] has proposed the model to investigate the pedestrians' behavior during such panic and jamming condition. Extended static floor field using *dijkstra algorithm* has been done by Katsuhiko Nishinari. His model is implemented on large room to avoid obstacles [11].

3. ORIGINALITY

In this study, we propose a new model approach by modifying the structure of the *static floor field* [1]. The proposed method is by defining Graph in calculating the distribution value of the *static floor field*. This study divides the evacuation process into several stages. Evacuation process is divided into two stages: (1) Stage 1: every pedestrian in the room of the building is trying to get out of every room (*using previous model*); (2) Stage 2: after the people get out of the room, the pedestrians will enter more complex room (*corridors of the building*). At this stage, new approach will be implemented.

4. SYSTEM DESIGN

This study analyzes the behavior of pedestrians in a building when a disaster occurs. When disaster strikes, panic disorder might potentially become a problem in the evacuation process. If pedestrians are inside a building, naturally they will immediately look for a safe area by using their basic knowledge. This study applies model of pedestrian dynamic in large room from previous researches by adding some modifications. This model uses cellular automata as a basic model for modeling to represent pedestrians. The model combines the Graph to find the shortest distance from the exit of *static floor field*. This model is expected to provide a solution in this study.

The basic model in this study uses a 3x3 matrix as neighboring cells. Each matrix is divided into two types. Type 1 represents the probability of a pedestrian s/he does not to move to a neighboring cell. Meanwhile, Type 2 has eight-cells to represent the probability of a pedestrian to move to a neighboring cell. One of the neighboring cells will be occupied by pedestrians when they move to the neighboring cell.

4.1 Floor Field

Floor field in this model consists of two types [1] [2] [3], namely *dynamic floor field* and *static floor field*. Dynamic floor field represents the interaction between pedestrians. The value of dynamic floor field will be

affected by the movement of the pedestrians when they have moved to a neighboring cell. The value of dynamic floor field occupied by pedestrians will be increased by 1. Dynamic floor field is influenced by two parameters, namely *diffusion* and *decay*. Static floor field has a fixed value. In the previous research, the weight of static floor field is calculated by using an equation to find the shortest distance. When getting closer to the exit, the weight of the static floor field will become larger. Static floor field value can be calculated by using the following equation (1):

$$S_{ij} = \min_{(i\tau_s, j\tau_s)} \left\{ \max_{(il, jl)} \left\{ \sqrt{(i\tau_s - i_l)^2 + (j\tau_s - j_l)^2} \right\} - \sqrt{(i\tau_s - i)^2 + (j\tau_s - j)^2} \right\} \quad (1)$$

The equation (1) was introduced by Angsar K (2002). Equation 1 can be used to calculate the weight of the static floor field, for example, in the case occurring in a large room. That equation is good for modeling case of evacuation in large room where there are no obstacles. Modeling in a large room provides obstacles that might make pedestrians stuck on an obstacle. To avoid obstacles, Kanishiro [11] introduced a modification of static floor field by using graph. Graph is made using the corners of obstacles which are interconnected with one another. For the proposed model, the graph is defined by the researcher. In this study, the structure of the building is very complicated. It would make the weight distribution become more complicated for static floor field.

4.2 Probability to Move

C. Burstedde [1] introduced a method in determining the direction of the movement of pedestrians into a neighboring cell by using probability theory. It can be seen on the following equation (2):

$$P_{ij} = NM_{ij} D_{ij} S_{ij} (1 - n_{ij}) \quad (2)$$

- P_{ij} : Probability to move
- N : Normalization factor
- M_{ij} : Matrix preferences
- D_{ij} : Value of matrix dynamic floor field at index i, j .
- S_{ij} : Value of matrix static floor field at index i, j .
- n_{ij} : Indicator of neighboring cell, 1 if any pedestrian and 0 if empty

Angsar K. made some modifications to the equations introduced by C Burstedde. He is more focused on the impact caused by sensitive parameters (ks and kd). Both parameters are inserted into the equation (2) to give the effect of herding and blind behavior of the pedestrians. The equation has changed as into the following equation (3).

$$P_{ij} = N \exp(k_D D_{ij}) \exp(k_S S_{ij})(1 - n_{ij})\epsilon_{ij} \tag{3}$$

The ϵ_{ij} has the value of 0 if the cell is a wall or obstacle. K_s is a sensitive parameter for *static floor field* and k_d is a sensitive parameter for *dynamic floor field*. This study is intended to see the influence of k_s and k_d in an evacuation if the experiment is conducted in a building.

4.3. Solving problem when two or more people enter the same space

Parallel update allowstwo or more pedestrians went into the same space. This condition would create conflict in the process of updating the rules. When a conflict arises, the equation in Figure 1 and 2 can be used to resolve the problem. In regard to the previous research, the number of neighboring transition matrix was 4 or 8, but in this case the researcher used8neighboring transition matrices.

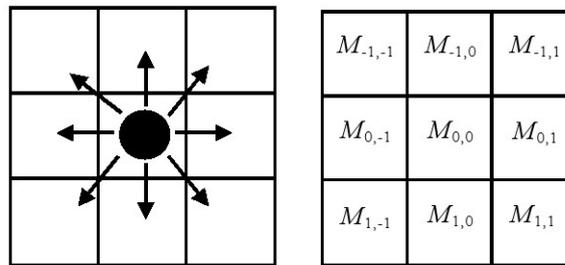


Figure 1. A particle has the possibility to move to the neighboring matrix $M = (M_{ij})$ [1].

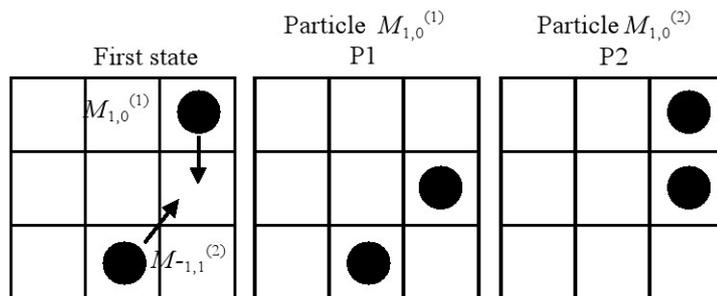


Figure 2. Solution if there are two pedestrians ($M^{(1)}$ and $M^{(2)}$) moving to the same neighbor cell.

$$P1 = \frac{M_{1,0}(1)}{M_{1,0}(1) + M_{1,0}(2)}$$

$$P2 = \frac{M_{1,0}(2)}{M_{1,0}(1) + M_{1,0}(2)}$$

The above conditions are used when there are two or more pedestrians moving into the same cell in one time space.

4.4 Update Rule

In applying this method, some rules such as the ones used in the previous studies were used [1] [2] [3]. The following rules are applied to each pedestrian based on parallel update in discrete time step ($t \rightarrow t + 1$):

1. Dynamic floor field controlled by *diffusion* and *decay* processes.
2. Each pedestrian has a transition probability to move to another neighbor cell which is determined by Equation⁽²⁾ and will be influenced by two sensitive parameters $ks \in [0, \infty]$ and $kd \in [0, \infty]$.
3. Every pedestrian will move to a neighboring cell based on the transition probability of the previous step.
4. If there are two or more pedestrians who chose the same cell targets, this problem will be solved by the above method^(2.1).
5. Dynamic floor field value will increase by the movement of pedestrians ($D \rightarrow D+1$).

The rules above are used to update the movement of all pedestrians at the same time space in parallel update.

4.5. Panic Behavior

One of the interesting things in evacuation process is the sense of panic experienced by the individual. This panic phenomenon during the occurrence of disaster has some effects towards the evacuation and it makes the evacuation process become more complicated. In the process of evacuation, panic behavior often leads to death. Their panic might cause them to stumble, fall or get trampled by others [4]. This study tries to insert some of the characteristics of panic behavior into the simulation. The previous studies have described some of the characteristics of panic behavior when a disaster strikes. This experiment does not use all the characteristics of panic behavior. This experiment uses some limitations by using only a few panic characteristics to this simulation, which are:

- Getting nervous and acting blindly.
- Running faster than normal pedestrian.
- Showing herding behavior, which is by following each other, especially the larger group.
- Pushing each other at any exits while alternative exits are often not efficient for them to escape.

The research was conducted by Angshar K (2002). The parameter ks and kd have some effects in representing the panic behaviors. The lower the value of ks means the higher the chance of pedestrians acting blindly in looking for the exit and it means they will show more random behaviors, such as running mindlessly. The higher value of ks means that the pedestrians know better about the exit position and the surrounding

environment. The higher the value of kd means that the pedestrians show herding behavior. To represent the behavior of panic that has been described previously, this study uses the combination of kd and ks values.

4.6. Proposed Concept

In Computer science, graph is defined as a structure used to model pairwise relations between objects. The interconnected objects are represented by mathematical abstractions called vertices, and the links that connect some pairs of vertices are called edges. Graph $(G = \langle V, E \rangle)$ consists of unit of vertices (V) and unit of edges (E). Edge formulation $(E = (u, v))$ means that Edge (e) is connected by two points, which are u and v . To make the computation easier, this study uses directed graphs.

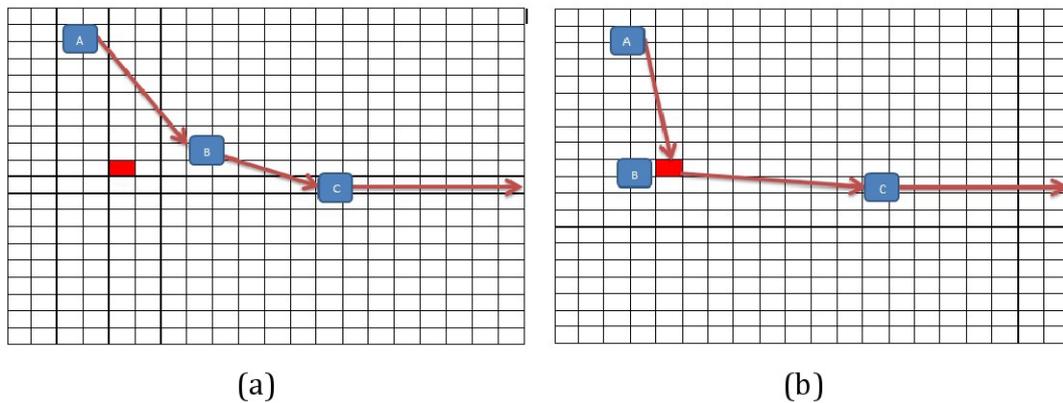


Figure 3. (a) Initial of cell, (b) Calculate value of cell

Figure 3 describes how the graph is used to calculate the distance to the nearest exit. In the previous study [2], the simulation is performed only in a room. To calculate the value of *static floor field*, the researcher used Euclidean equation to find the shortest distance to the exit. Steps for calculating the value of *static floor field* of the proposed method is described as follows:

1. Defining the position of Matrix (M_{ij}) of the sequence of the cell. Figure 5 is illustrated in the red cell.
2. Finding the nearest vertices or nodes, which—in the example above—is vertices B .
3. Replacing the nearest position of vertices (V_i) with the position of matrix (M_{ij}) cell.
4. Calculating new edge distance of replaced vertices.
5. Calculating total distance of the nearest exit.
6. Repeating steps 1-5 until the last cell.

Weight edge $E = (u, v)$ is calculated by using Equation 4.

$$WE_i = \sqrt{(u_i - v_i)^2 + (u_j - v_j)^2} \quad (4)$$

In which :

- WE_i = Weight of egde i .
- u_i and u_j = Position of the first vertices (V) on Matrix (M_{ij} .)
- v_i and v_j = Position of the second vertices (V) on Matrix (M_{ij} .)

When the value of WE is already found, the nearest Vertices (V_{ij}) to cell of Matrix (M_{ij}) is computed by using Equation 5.

$$NV = \min\{\sqrt{(x_i - xv_i)^2 + (y_j - yv_j)^2}\} \quad (5)$$

In which :

- NV = Nearest weight of new Vertices.
- x_i and y_j = Position of the cell on Matrix M_{ij} .
- xv_i and yv_j = Position of the vertices V_i on Matrix M_{ij} .

NV is the closest distance value between matrix M_{ij} and Vertices V_i . We can calculate the value of all the edges connected with Vertices V_i , and then calculate all the possible paths toward an exit and find the closest value with Equation 6.

$$TW_{ij} = \min\{NV + \sum_{i=0}^n WE_i\} \quad (6)$$

TW_{ij} is the total value of distance Matrix (M_{ij}) to the nearest exit door. Equation 5 and 6 are implemented on all iterations while Equation 4 is only implemented once, at the first time when running the application.

4.7. Map in Case Study

This research combines the proposed methods and the previous methods for evacuation in a building. The location chosen as the model to conduct this virtual experiment was Marina Plaza, Surabaya, Indonesia considering that Marina Plaza is one of the shopping malls in Surabaya which has relatively frequent number of visitors. The details of the view and map of Plaza Marina Surabaya can be seen in Figure 4.

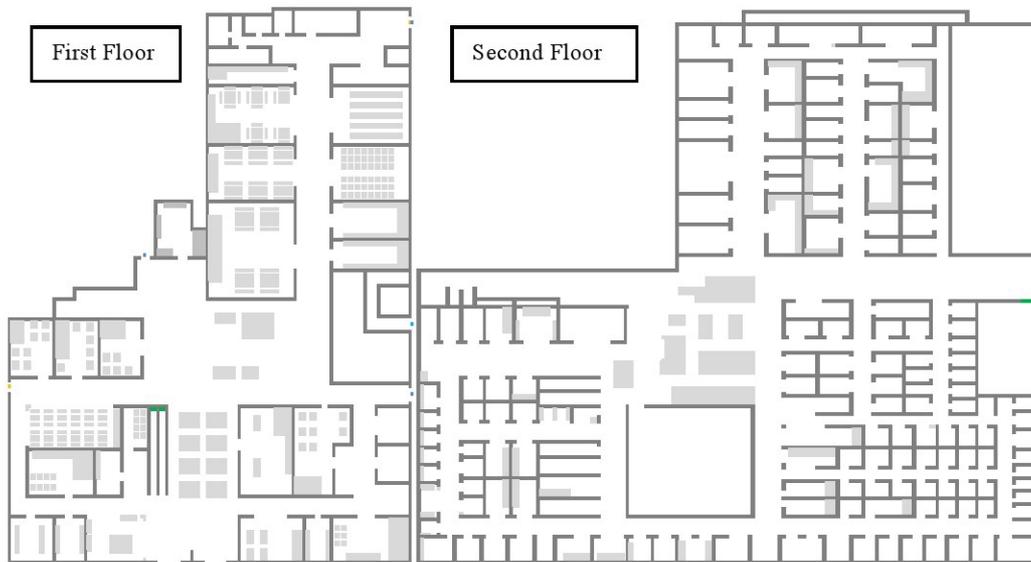


Figure 4. Map of Marina Plaza Surabaya

5. EXPERIMENT AND ANALYSIS

This section will discuss the impact of sensitive parameters (ks and kd) that are inserted into this simulation. This experiment is divided into three parts: *Comparison between the Previous and the Proposed Methods Related to Static Floor Field*, *Simulation of Evacuation based on the Panic and Normal Characters*, and *Simulation of Evacuation using Actual Data*.

5.1 Comparison between the Previous and the Proposed Methods Related to Static Floor Field

To see the performance of the proposed method, this section will compare the previous method[1] and the proposed method. Virtual experiment was conducted by making simulation in large rooms with the same specifications by using some obstacles as seen in the maps below:



Figure 5. Two maps(a) and (b) to compare the previous and the proposed method.

Figure 5 shows two maps used for comparison between the previous and proposed method. The specifications of the room can be seen in the list below:

1. Size of the room is 73 X 65 cells and the room has one door.
2. Size of the door is 5 cells.
3. The area of each cell is 40x40 cm²

The proposed method to solve the problem when there is any obstacle in front of door can be seen in the Figure 6 and 7 below.

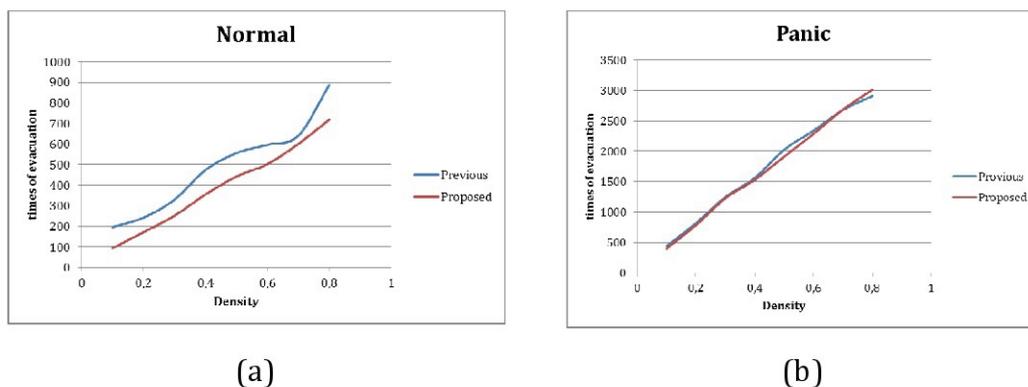


Figure 6. Relational graphics of evacuation time and *density* of both normal and panic pedestrians.

According to the relational graphics, simulation modeling in normal conditions is shown in Figure 6 (a). The evacuation time difference between the previous and the proposed method is quite high because in this situation the pedestrians have a good knowledge to find the exit. This condition makes the view of pedestrians only focused toward the exit. This condition makes them get stuck on obstacles and it becomes difficult for them to find the exit if there are obstacles in front of the door. In Figure 6 (b), the evacuation time difference between the previous and the proposed method is quite low. Pedestrians in panic situation tend to be nervous and act blindly. This condition makes them walk or run randomly and mindlessly. In this condition, there would be a low tendency to get stuck on an obstacle. As a consequence, the evacuation time gap between the two methods is low, yet the evacuation time needed in panic situation highly increases.

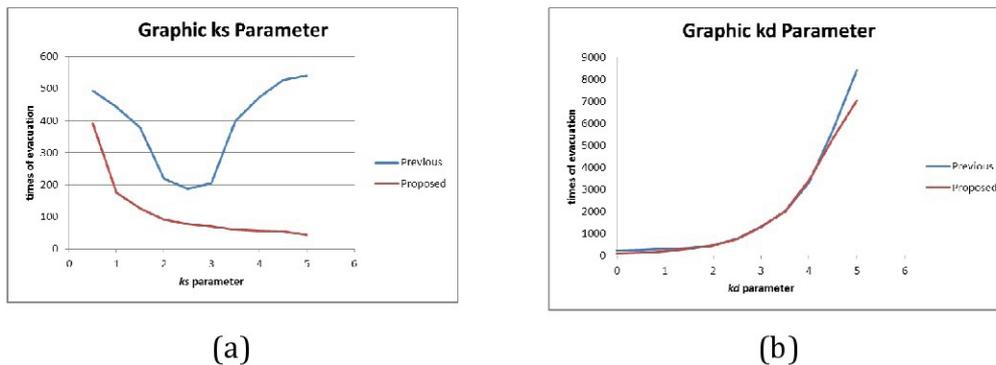


Figure 7. Relational graphics of evacuation time, kd and ks .

Ks parameter represents the pedestrians' knowledge on the location of the exit. Adding obstacles in the large room simulation will result in higher evacuation time in certain conditions given that some pedestrians are trapped by obstacles and it becomes difficult for them to find the exit. In Figure 7 (a), the evacuation time does not decrease regularly. When the value of $ks=3$, evacuation time increases. In this condition, evacuation time is supposed to decrease regularly [1]. The higher value of kd , pedestrians will follow each other (*herding behaviors*) and act blindly. In this condition, the possibility of the pedestrian to get trapped becomes smaller, yet the evacuation time will consequently increase. In Figure 7 (b), the time difference evacuation between the previous method and the proposed method is quite small.

5.2. Simulation of Evacuation based on the Panic and Normal Characters

In the previous studies, the effect of ks and kd in the large room was studied by Angsar K. If ks is lower than 1, it means that the pedestrians do not have enough knowledge about the environment. It suggests that the pedestrians are confused to find the exit and assume that the room is full of smoke, in case of fire. If ks parameter is bigger than 1, it means the pedestrians have enough knowledge about the environment and know the location of exit. Meanwhile, kd parameter has different influences. If kd is higher than 1, Kd parameter has the effect of making the pedestrians lead and follow each other. In this experiment, the characteristic of pedestrians has been divided into two characters by using the combination of ks and kd . This combination is made to divide the characteristics of the pedestrians when they are in normal situation and when they are in panic. For more details, it can be seen below:

Panic Character : ks parameter is 1 and kd parameter is 2
 Normal Character : ks parameter is 2 and kd parameter is 1

The above combination is one of the examples of combinations that would be modelled. The value range of ks and kd in the previous research is 0

to infinite. However, the researcher will still refer to the previous statement on how the impact would be if the k_d and k_s value is higher. Hence the combination of k_s and k_d such as above is chosen to represent the character of the pedestrians in panic and normal situation.

The simulations have been done by using real data from Marina Plaza Surabaya on the first and the second floors. The second floor is one of the most crowded areas. Evacuation route in this building has already been determined by Marina Plaza Surabaya. This experiment will be based on the data of the evacuation route of Marina Plaza Surabaya. The specifications of the simulation can be seen below:

1. The area of each cell is $40 \times 40 \text{ cm}^2$
2. The number of exits is six doors.
3. The size of the building is 179×217 cells and the experiment only uses the first and the second floors.
4. The case study is situated at one of the shopping centers in Surabaya.
5. The plaza building has 3 floors but this case study takes place on the first and the second floors.
6. The evacuation route is based on the emergency evacuation route of Marina Plaza Surabaya.

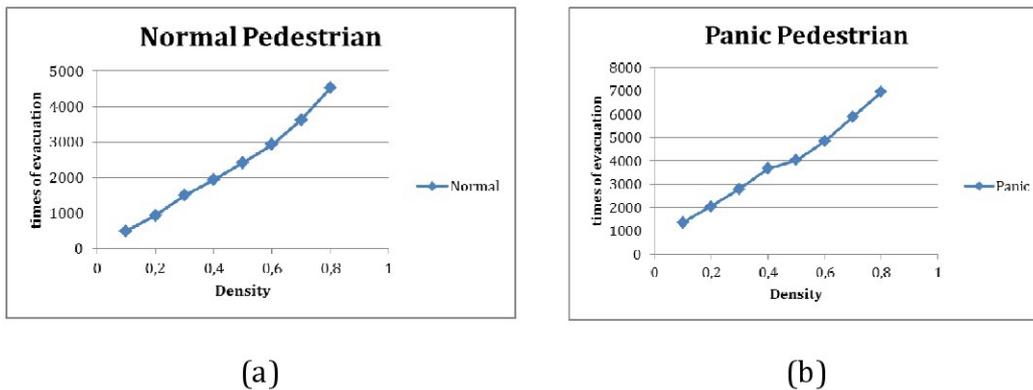


Figure 8. (a) Route of evacuation on the first floor, (b) Route of evacuation on the second floor

This experiment is based on the evacuation route of Marina Plaza Surabaya. The meaning of "*evacuation route*" is the evacuation route used by Marina Plaza Surabaya when disaster occurs. In general, all the buildings have emergency evacuation standards, but every building management should have emergency evacuation standards adapted to their building

standards. This study has followed the routes of evacuation at Marina Plaza Surabaya. Details of the evacuation route can be seen in Figure 8. Figure 8(a) is the first floor and Figure 8(b) is the second floor.

This simulation uses two above characters: in panic and normal situation. These characters have been inserted into the modeling. For more details of the result of the experiment, see Figure 9 below.



(a) (b)
Figure 9. Relational graphics of evacuation time and *density* proposed method.

Figure 9 (a) is an experiment to find the relation between time of evacuation and density of normal characteristics. Basically, greater value of density will be followed by increased evacuation time. Figure 9 (b) is an experiment to find the relation between time of evacuation and density for pedestrians with panic character. In this experiment, greater value of density will be followed by increased evacuation time. When looking into the two graphics above it can be concluded that the two graphics above have the same characteristics, but they have different value of evacuation time.

5.3. Simulation of Evacuation using Actual Data

This section is intended to determine the evacuation time by using actual data. Shopping centers, particularly Marina Plaza Surabaya, has a different number of visitors during normal (*weekdays*) and weekends/public holidays. Surabaya Local Government has divided shopping center activities into three parts: *low density* (visitors on Monday, Tuesday, and Wednesday), *middle density* (visitors on Thursday and Friday), and *high density* (visitors on Saturday and Sunday (*weekend*)).

Table 1. Number of Visitors on one Week

Num	Category	Number of Visitors
1	Low	929/hour
2	Middle	933/hour
3	High	1164/hour

Table 1 is the estimation of the number of visitors at Marina Plaza Surabaya in one week. The number of visitors is calculated by the number of cars and bicycles parked at Marina Plaza Surabaya's parking lot. The number of visitors used is only that in the first and second floors. The most crowded floor is the second floor because the second floor is the center of Marina Plaza Surabaya. According to Table 1, the difference between the number of visitors in the category of *Low* and *Middle* are not high. The number of visitors in Table 1 is the average number of visitors per hour. To see the results of the experiment, we can see the graphics below.

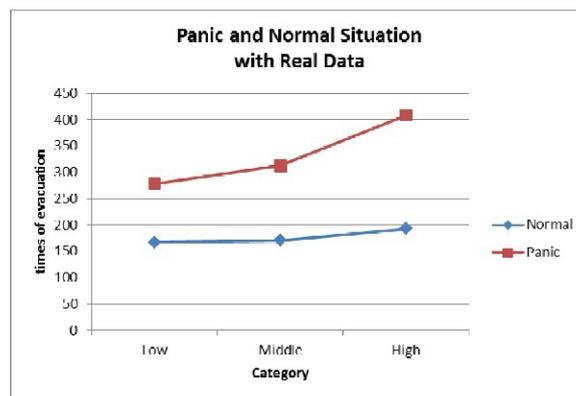


Figure 10. Relational graphics between Panic and Normal Pedestrians using Actual Data.

According to the graphic in Figure 10, the evacuation time in Low and Middle category have small difference. The characteristics number of visitors of Marina Plaza Surabaya on Monday to Friday does not show high increase. However, during weekend, the number of visitors has increased quite a lot. This condition makes the evacuation time falls to the category of *High* because the time increases quite a lot (see Figure 10). The experimental results by using the actual data show the same tendency of evacuation time, yet the panic character has higher evacuation time than normal characters.

6. CONCLUSION

Basic model proposed by C. Burstedde can be implemented to modeling evacuation process in a building by using some modifications of *static floor field*. This study modifies the distribution of *static floor field* from the previous study so the proposed method can be applied in a building. The experiment shows that the proposed method works better than the previous method when applied in certain condition. The calculation of the distribution value of *static floor field* can be implemented by using Graph. Graph is used to give direction to pedestrians to follow the *evacuation route* in a building, in this case Marina Plaza Surabaya. According to the experiment results, it can be concluded that defining the direction of Graph is very important in determining the duration of evacuation time. By using the modification of *static floor field*, it shows that proposed method can be implemented on

evacuation process in a building. This model is expected to help analyze the panic behavior of pedestrians when disaster occurs, particularly at Marina Plaza Surabaya. By implementing this method, it is hoped that in the future management of buildings for public facilities could design much better systems of evacuation standards especially for the safety of the visitors.

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